

Exploring post-quantum cryptography in Internet protocols

Douglas Stebila



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WATERLOO



**NSERC
CRSNG**

<https://eprint.iacr.org/2019/858>

<https://eprint.iacr.org/2019/1356>

<https://eprint.iacr.org/2019/1447>

<https://tools.ietf.org/html/draft-stebila-tls-hybrid-design-01>

<https://openquantumsafe.org/>

<https://github.com/open-quantum-safe/>

<https://www.douglas.stebila.ca/>



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IQC Institute for
Quantum
Computing

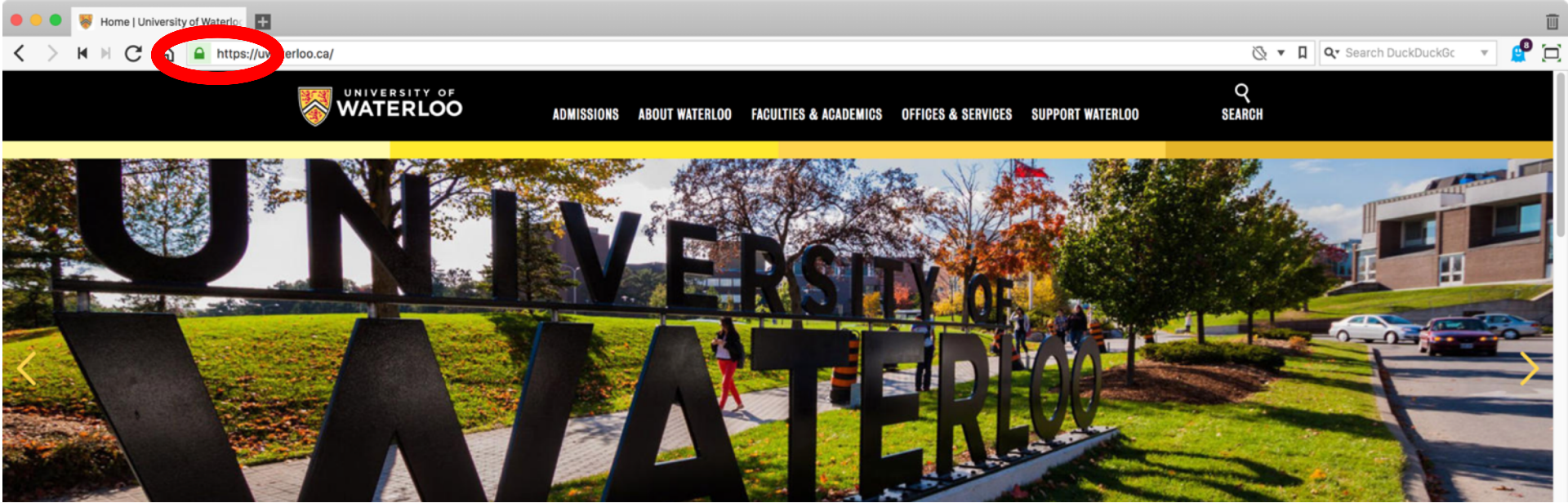


CYBER INSTITUTE
SECURITY
AND PRIVACY
UNIVERSITY OF WATERLOO

Post-quantum crypto @ Waterloo

- UW involved in 6 NIST Round 2 submissions:
 - CRYSTALS-Kyber, FrodoKEM, NewHope, NTRU, SIKE; qTESLA
- Large team led by David Jao working on isogeny-based crypto
- Quantum cryptanalysis led by Michele Mosca
- CryptoWorks21 training program for quantum-resistant cryptography

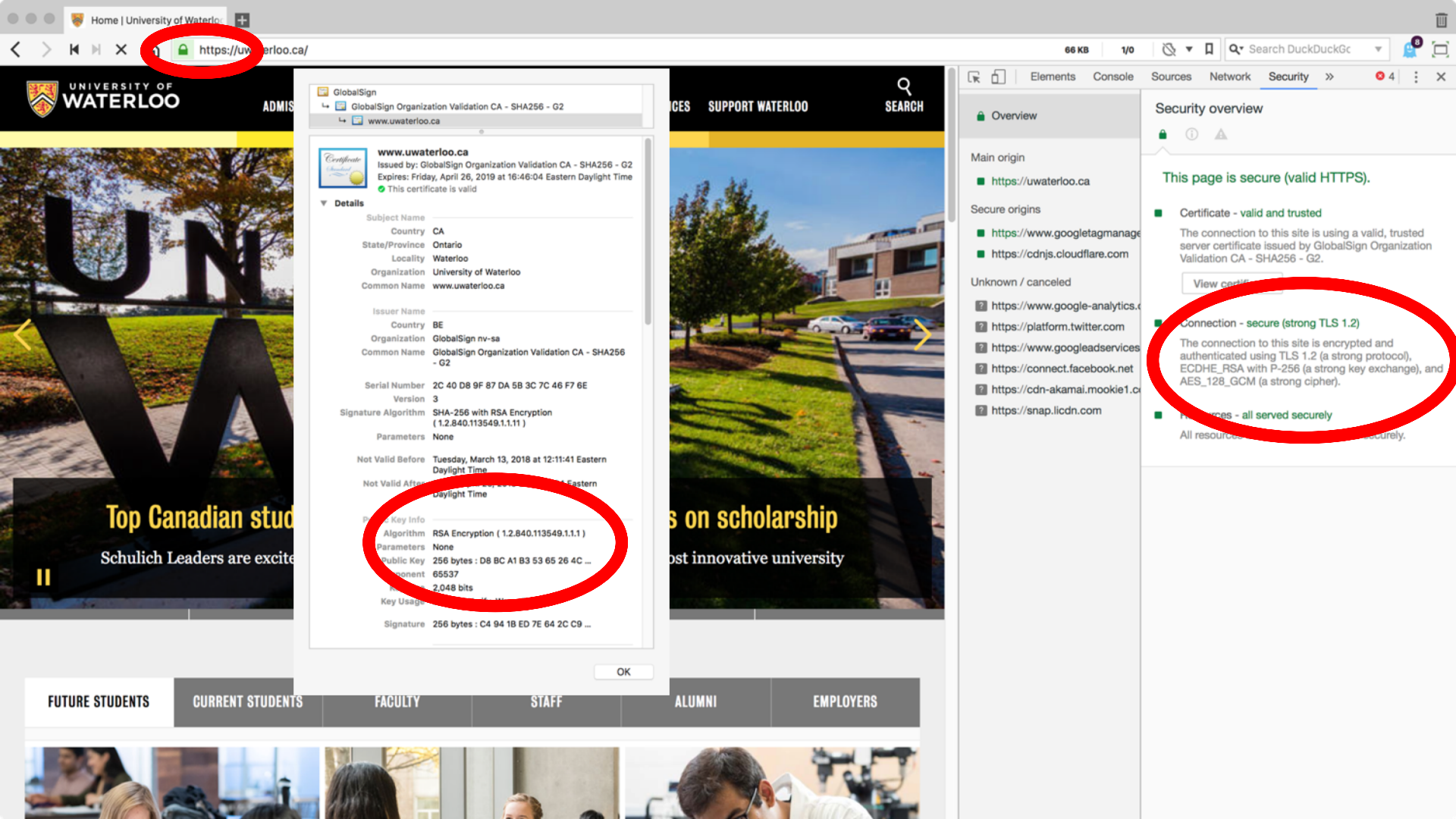
Motivating post-quantum cryptography



TLS (Transport Layer Security) protocol

a.k.a. SSL (Secure Sockets Layer)

- The “s” in “https”
- **The most important cryptographic protocol on the Internet** — used to secure billions of connections every day.



https://www.uwaterloo.ca/

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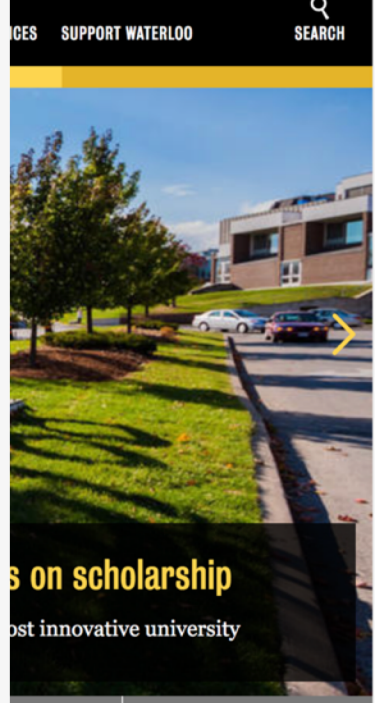
GlobalSign
GlobalSign Organization Validation CA - SHA256 - G2
www.uwaterloo.ca

www.uwaterloo.ca
Issued by: GlobalSign Organization Validation CA - SHA256 - G2
Expires: Friday, April 26, 2019 at 16:46:04 Eastern Daylight Time
This certificate is valid

Details

Subject Name	
Country	CA
State/Province	Ontario
Locality	Waterloo
Organization	University of Waterloo
Common Name	www.uwaterloo.ca
Issuer Name	
Country	BE
Organization	GlobalSign nv-sa
Common Name	GlobalSign Organization Validation CA - SHA256 - G2
Serial Number	2C 40 D8 9F 87 DA 5B 3C 7C 46 F7 6E
Version	3
Signature Algorithm	SHA-256 with RSA Encryption (1.2.840.113549.1.1.1)
Parameters	None
Not Valid Before	Tuesday, March 13, 2018 at 12:11:41 Eastern Daylight Time
Not Valid After	Tuesday, April 24, 2019 at 16:46:04 Eastern Daylight Time
Key Info	
Algorithm	RSA Encryption (1.2.840.113549.1.1.1)
Parameters	None
Public Key	256 bytes : D8 BC A1 83 65 26 4C ...
Exponent	65537
Modulus	2,048 bits
Key Usage	
Signature	256 bytes : C4 94 1B ED 7E 64 2C C9 ...

OK



66 KB 1/0 Search DuckDuckGo

Elements Console Sources Network Security

Overview

Main origin

- https://www.uwaterloo.ca

Secure origins

- https://www.googletagmanager.com
- https://cdnjs.cloudflare.com

Unknown / canceled

- https://www.google-analytics.com
- https://platform.twitter.com
- https://www.googleadservices.com
- https://connect.facebook.net
- https://cdn-akamai.mookie1.com
- https://snap.licdn.com

Security overview

This page is secure (valid HTTPS).

- Certificate - valid and trusted
The connection to this site is using a valid, trusted server certificate issued by GlobalSign Organization Validation CA - SHA256 - G2.
View certificate
- Connection - secure (strong TLS 1.2)
The connection to this site is encrypted and authenticated using TLS 1.2 (a strong protocol), ECDHE_RSA with P-256 (a strong key exchange), and AES_128_GCM (a strong cipher).
- Resources - all served securely
All resources on this page were served securely.

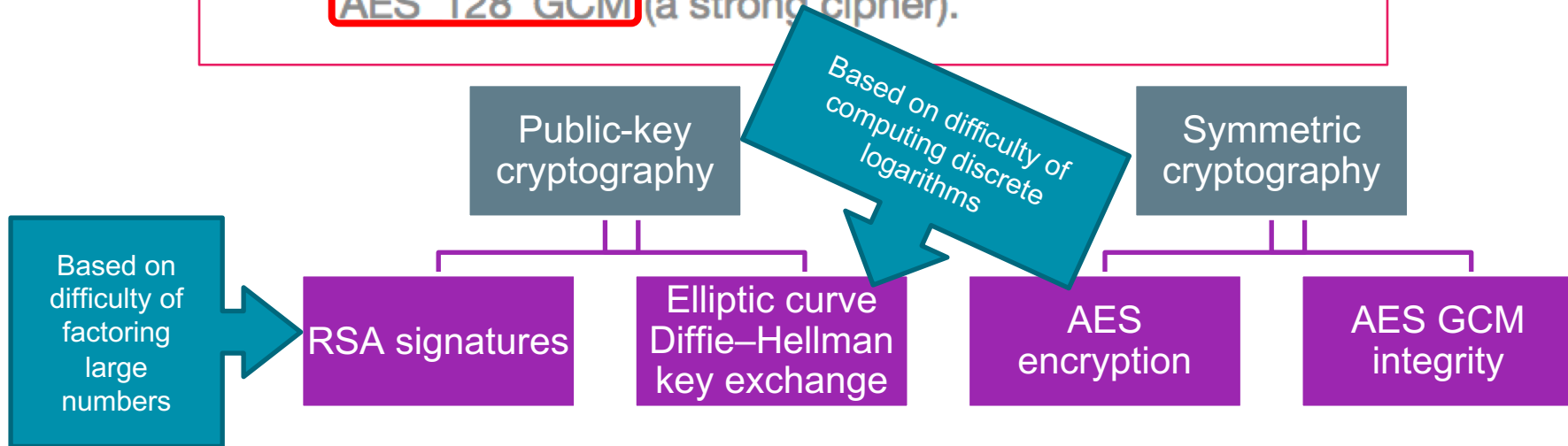
FUTURE STUDENTS CURRENT STUDENTS FACULTY STAFF ALUMNI EMPLOYERS



Cryptographic building blocks

- Connection - **secure (strong TLS 1.2)**

The connection to this site is encrypted and authenticated using TLS 1.2 (a strong protocol), **ECDHE RSA with P-256** (a strong key exchange), and **AES 128 GCM** (a strong cipher).



Quantum Starts Here



IBM Q



For researchers



For educators



For business



For developers

When will a large-scale quantum computer be built?

“I estimate a 1/7 chance of breaking RSA-2048 by 2026 and a 1/2 chance by 2031.”

— Michele Mosca, University of Waterloo
<https://eprint.iacr.org/2015/1075>



Post-quantum cryptography

a.k.a. quantum-resistant algorithms

Cryptography believed to be resistant to attacks by quantum computers

Uses only classical (non-quantum) operations to implement

Not as well-studied as current encryption

- Less confident in its security
- More implementation tradeoffs

Hash-based
& symmetric

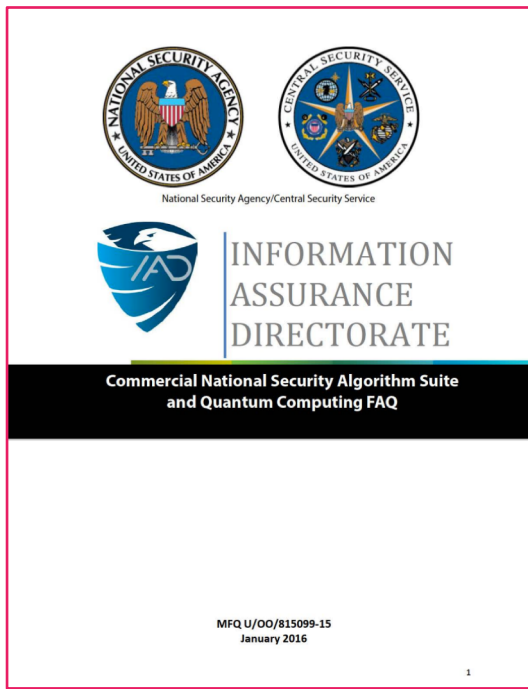
Multivariate
quadratic

Code-based

Lattice-
based

Elliptic curve
isogenies

Standardizing post-quantum cryptography



“IAD will initiate a transition to quantum resistant algorithms in the not too distant future.”

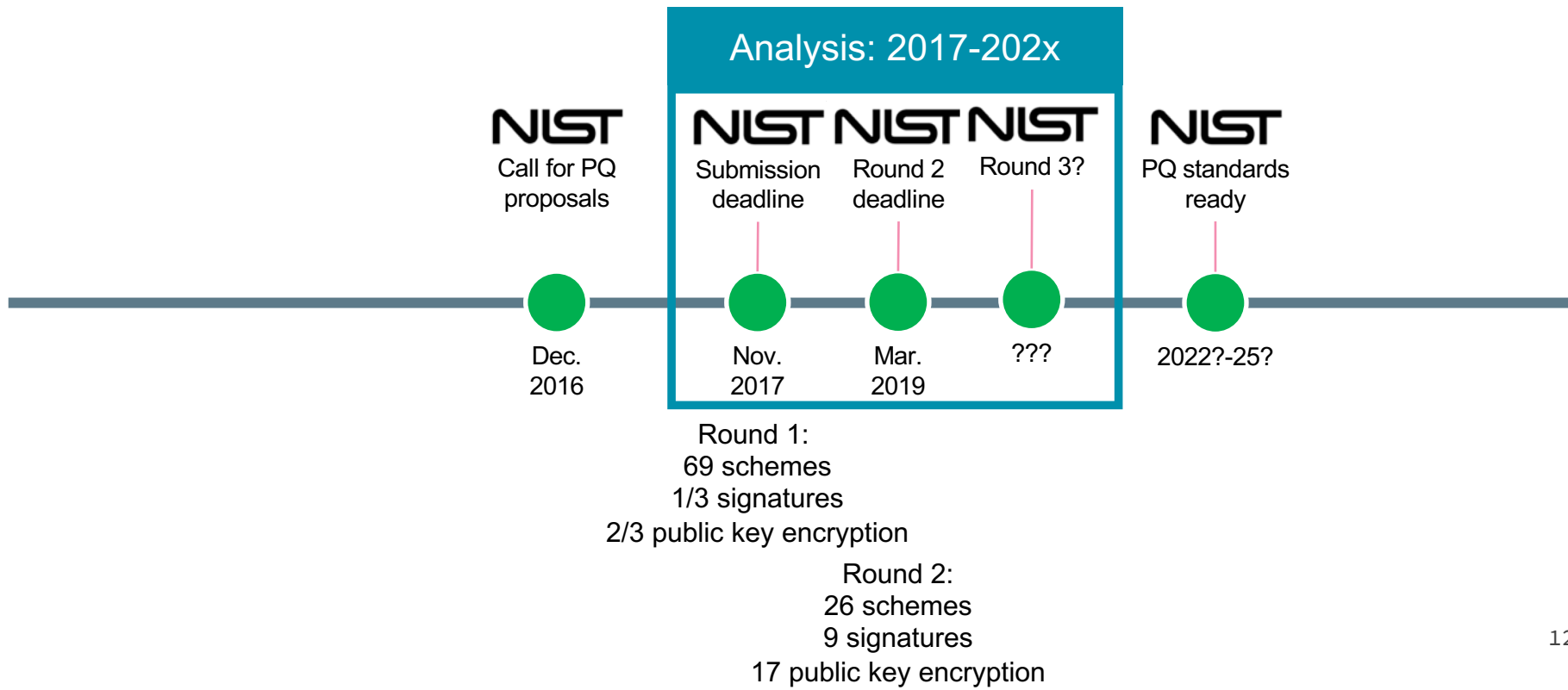
– NSA Information Assurance Directorate,
Aug. 2015

Aug. 2015 (Jan. 2016)



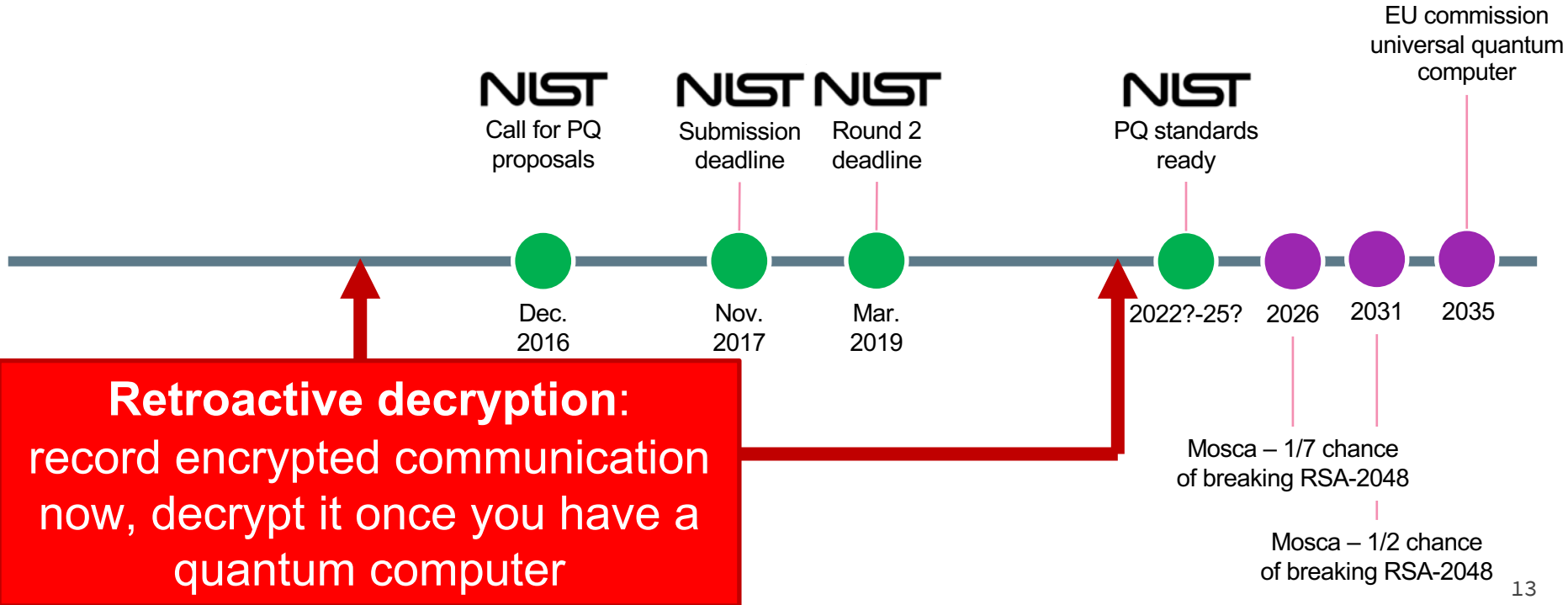
NIST Post-quantum Crypto Project timeline

<http://www.nist.gov/pqcrypto>



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NIST Post-quantum Crypto Project timeline

<http://www.nist.gov/pqcrypto>

NIST

SHA-1
standardized

SHA-1
weakened

NIST

SHA-2
standardized

NIST

PQ standards
ready

EU commission
– universal quantum
computer



1995

2001

2005

Jan.
2017

Aug.
2017

2022?-25?

2026

2031

2035



Browsers stop accepting
SHA-1 certificates



16 years

Mosca – 1/7 chance
of breaking RSA-2048

Mosca – 1/2 chance
of breaking RSA-2048

“Hybrid”

“Hybrid” or “composite” or “dual” or “multi-algorithm” cryptography

— — —

- Use pre-quantum and post-quantum algorithms together
- Secure if either one remains unbroken

Why hybrid?

- Potential post-quantum security for early adopters
- Maintain compliance with older standards (e.g. FIPS)
- Reduce risk from uncertainty on PQ assumptions/parameters

Hybrid ciphersuites

	Key exchange	Authentication
1	Hybrid traditional + PQ	Single traditional
2	Hybrid traditional + PQ	Hybrid traditional + PQ
3	Single PQ	Single traditional
4	Single PQ	Single PQ

Likely focus
for next 5-10 years

- Need PQ key exchange before we need PQ authentication because future quantum computers could retroactively decrypt, but not retroactively impersonate

Hybrid key exchange and authentication to date

- Hybrid key exchange Internet-Drafts at IETF:
 - TLS 1.2: Schanck, Whyte, Zhang 2016; Amazon 2019
 - TLS 1.3: Schanck, Stebila 2017; Whyte, Zhang, Fluhrer, Garcia-Morchon 2017; Kiefer, Kwiatkowski 2018; Stebila, Fluhrer, Gueron 2019
 - IPsec / IKEv2: Tjhai, Thomlinson, Bartlet, Fluhrer, Geest, Garcia-Morchon, Smyslov 2019
- Hybrid key exchange xperimental implementations:
 - Google CECPQ1, CECPQ2; Open Quantum Safe; CECPQ2b; ...
- Hybrid X.509 certificates:
 - Truskovsky, Van Geest, Fluhrer, Kampanakis, Ounsworth, Mister 2018

Design issues for hybrid key exchange in TLS 1.3

Douglas Stebila, Scott Fluhrer, Shay Gueron. **Design issues for hybrid key exchange in TLS 1.3. Internet-Draft.** Internet Engineering Task Force, July 2019. <https://tools.ietf.org/html/draft-stebila-tls-hybrid-design-01>

Goals for hybridization

— — —

1. Backwards compatibility
 - Hybrid-aware client, hybrid-aware server
 - Hybrid-aware client, non-hybrid-aware server
 - Non-hybrid-aware client, hybrid-aware server
2. Low computational overhead
3. Low latency
4. No extra round trips
5. No duplicate information

Design options

- How to negotiate algorithms
- How to convey cryptographic data (public keys / ciphertexts)
- How to combine keying material

Negotiation: How many algorithms?

2

≥ 2

Negotiation: How to indicate which algorithms to use

— — —

Negotiate each algorithm individually

1. Standardize a name for each algorithm
2. Provide a data structure for conveying supported algorithms
3. Implement logic negotiating which combination

Negotiate pre-defined combinations of algorithms

1. Standardize a name for each desired combination
 - Can use existing negotiation data structures and logic

Which option is preferred may depend on how many algorithms are ultimately standardized.

Conveying cryptographic data (public keys / ciphertexts)

1) Separate public keys

- For each supported algorithm, send each public key / ciphertext in its own parseable data structure

#1 requires protocol and implementation changes

#2 abstracts combinations into “just another single algorithm”

2) Concatenate public keys

- For each supported combination, concatenate its public keys / ciphertext into an opaque data structure

But #2 can also lead to sending duplicate values

- nistp256+bike11
 - nistp256+sikep403
 - nistp256+frodo640aes
 - sikep403+frodo640aes
- } 3x nistp256,
2x sikep403,
2x frodo640aes
public keys

Combining keying material

— — —

Top requirement: needs to provide “robust” security:

- Final session key should be secure as long as at least one of the ingredient keys is unbroken
- (Most obvious techniques are fine, though with some subtleties; see Giacom, Heuer, Poettering PKC’18, Bindel et al. PQCrypto 2019,)
- XOR keys
- Concatenate keys and use directly
- Concatenate keys then apply a hash function / KDF
- Extend the protocol’s “key schedule” with new stages for each key
- Insert the 2nd key into an unused spot in the protocol’s key schedule

Draft-00 @ IETF 104

draft-stabila-tls-hybrid-design-00

Contained a “menu” of design options along several axes

1. How to negotiate which algorithms?
2. How many algorithms?
3. How to transmit public key shares?
4. How to combine secrets?

Feedback from working group:

- Avoid changes to key schedule
- Present one or two instantiations
- Specific feedback on some aspects



Draft-01 @ IETF 105

draft-stebila-tls-hybrid-design-01

Kept menu of design choices

Constructed two candidate instantiations from menu for discussion

1. Directly negotiate each hybrid algorithm; separate key shares
2. Code points for pre-defined combinations; concatenated key shares

Additional KDF-based options for combining keys

Emerging consensus?

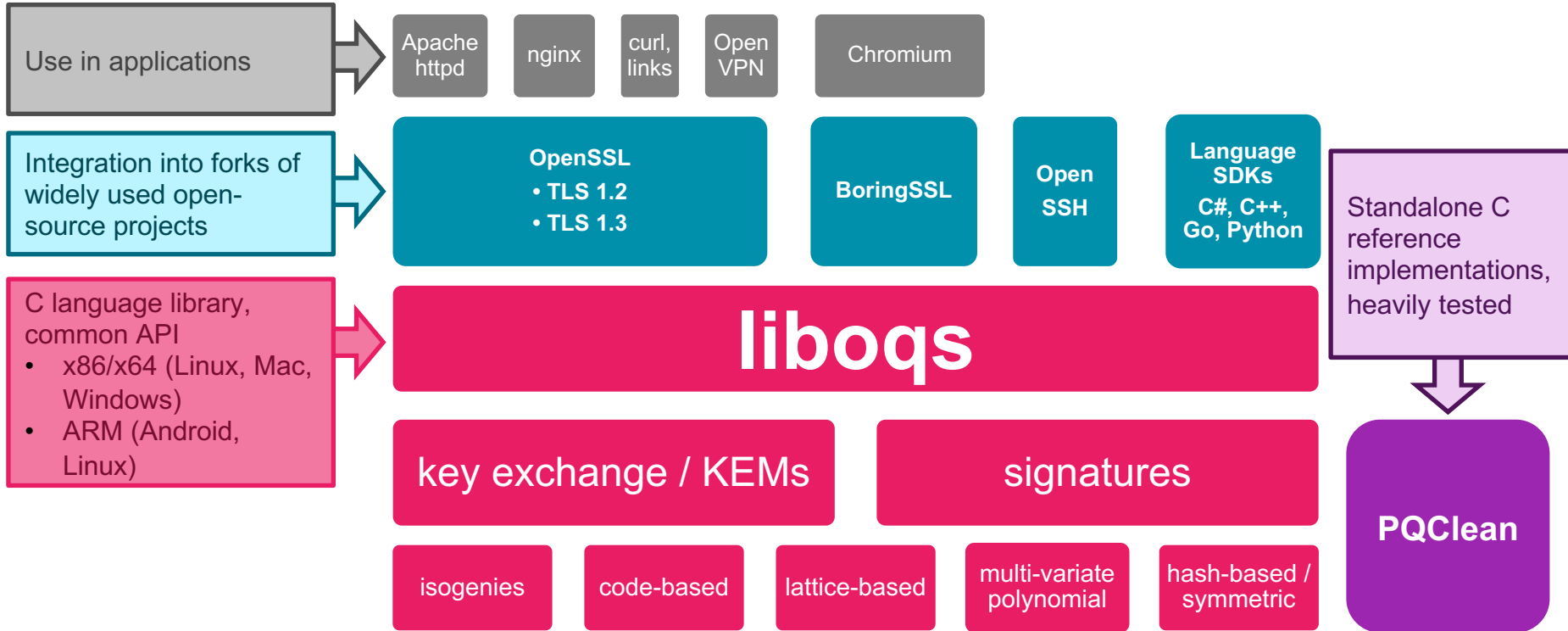
— — —

- **Combining keying material:**
 - Consensus: (unambiguously) concatenate keys then apply hash function / KDF
- **Number of algorithms:** 2 vs ≥ 2 :
 - TLS working group leaning to 2
- **Negotiation:** negotiate algorithms separately versus in combination:
 - All(?) implementations to date have negotiated pre-defined combinations
 - TLS working group leaning to “in combination”
- **Conveying public keys:** separately versus concatenated:
 - All(?) implementations to date have used concatenation
 - TLS working group leaning to (unambiguous) concatenation

OPEN QUANTUM SAFE

*software for prototyping
quantum-resistant cryptography*

Open Quantum Safe Project



OQS team

— — —

- Project leads
 - Douglas Stebila (Waterloo)
 - Michele Mosca (Waterloo)
- Industry collaborators
 - Amazon Web Services
 - Cisco Systems
 - evolutionQ
 - IBM Research
 - Microsoft Research
- Individual contributors
- Financial support
 - Government of Canada
 - NSERC Discovery
 - Tutte Institute
 - Amazon Web Services
- In-kind contributions of developer time from industry collaborators

liboqs

— — —

- C library with common API for post-quantum signature schemes and key encapsulation mechanisms
- MIT License
- Builds on Windows, macOS, Linux; x86_64, ARM v8
- 43 key encapsulation mechanisms from 7 NIST Round 2 candidates
- 52 signature schemes from 5 NIST Round 2 candidates

List of algorithms

Key encapsulation mechanisms

- **BIKE:** BIKE1-L1-CPA, BIKE1-L3-CPA, BIKE1-L1-FO, BIKE1-L3-FO
- **FrodoKEM:** FrodoKEM-640-AES, FrodoKEM-640-SHAKE, FrodoKEM-976-AES, FrodoKEM-976-SHAKE, FrodoKEM-1344-AES, FrodoKEM-1344-SHAKE
- **Kyber:** Kyber512, Kyber768, Kyber1024, Kyber512-90s, Kyber768-90s, Kyber1024-90s
- **NewHope:** NewHope-512-CCA, NewHope-1024-CCA
- **NTRU:** NTRU-HPS-2048-509, NTRU-HPS-2048-677, NTRU-HPS-4096-821, NTRU-HRSS-701
- **SABER:** LightSaber-KEM, Saber-KEM, FireSaber-KEM
- **SIKE:** SIDH-p434, SIDH-p503, SIDH-p610, SIDH-p751, SIKE-p434, SIKE-p503, SIKE-p610, SIKE-p751, SIDH-p434-compressed, SIDH-p503-compressed, SIDH-p610-compressed, SIDH-p751-compressed, SIKE-p434-compressed, SIKE-p503-compressed, SIKE-p610-compressed, SIKE-p751-compressed

Signature schemes

- **Dilithium:** Dilithium2, Dilithium3, Dilithium4
- **MQDSS:** MQDSS-31-48, MQDSS-31-64
- **Picnic:** Picnic-L1-FS, Picnic-L1-UR, Picnic-L3-FS, Picnic-L3-UR, Picnic-L5-FS, Picnic-L5-UR, Picnic2-L1-FS, Picnic2-L3-FS, Picnic2-L5-FS
- **qTesla:** qTesla-p-I, qTesla-p-III
- **SPHINCS+-Haraka:** SPHINCS+-Haraka-128f-robust, SPHINCS+-Haraka-128f-simple, SPHINCS+-Haraka-128s-robust, SPHINCS+-Haraka-128s-simple, SPHINCS+-Haraka-192f-robust, SPHINCS+-Haraka-192f-simple, SPHINCS+-Haraka-192s-robust, SPHINCS+-Haraka-192s-simple, SPHINCS+-Haraka-256f-robust, SPHINCS+-Haraka-256f-simple, SPHINCS+-Haraka-256s-robust, SPHINCS+-Haraka-256s-simple
- **SPHINCS+-SHA256:** SPHINCS+-SHA256-128f-robust, SPHINCS+-SHA256-128f-simple, SPHINCS+-SHA256-128s-robust, SPHINCS+-SHA256-128s-simple, SPHINCS+-SHA256-192f-robust, SPHINCS+-SHA256-192f-simple, SPHINCS+-SHA256-192s-robust, SPHINCS+-SHA256-192s-simple, SPHINCS+-SHA256-256f-robust, SPHINCS+-SHA256-256f-simple, SPHINCS+-SHA256-256s-robust, SPHINCS+-SHA256-256s-simple
- **SPHINCS+-SHAKE256:** SPHINCS+-SHAKE256-128f-robust, SPHINCS+-SHAKE256-128f-simple, SPHINCS+-SHAKE256-128s-robust, SPHINCS+-SHAKE256-128s-simple, SPHINCS+-SHAKE256-192f-robust, SPHINCS+-SHAKE256-192f-simple, SPHINCS+-SHAKE256-192s-robust, SPHINCS+-SHAKE256-192s-simple, SPHINCS+-SHAKE256-256f-robust, SPHINCS+-SHAKE256-256f-simple, SPHINCS+-SHAKE256-256s-robust, SPHINCS+-SHAKE256-256s-simple

PQClean

— — —

- New, sister project to OQS
- Goal: standalone, high-quality C reference implementations of PQ algorithms
 - Lots of automated code analysis and continuous integration testing
 - Builds tested on little-endian and big-endian
- MIT License and public domain
- Not a library, but easy to pull out code that can be incorporated into a library
 - liboqs consumes implementations from PQClean
- In collaboration with Peter Schwabe and team at Radboud University, Netherlands

<https://github.com/PQClean/PQClean>

OpenSSL

— — —

- OQS fork of OpenSSL 1.0.2
 - PQ and hybrid key exchange in TLS 1.2
- OQS fork of OpenSSL 1.1.1
 - PQ and hybrid key exchange in TLS 1.3
 - PQ and hybrid certificates and signature authentication in TLS 1.3
- Can be readily used with applications that rely on OpenSSL with few/no modifications

OQS demo: OpenSSL

```
build --bin/links /Users/dstebila/Desktop/build -- links https://localhost:4433/ -- 109x32
(p4 of 5)
ECDH-RSA-DES-CBC3-SHA ECDH-ECDSA-DES-CBC3-SHA DES-CBC3-SHA
Signature Algorithms: RSA+SHA512:DSA+SHA512:ECDSA+SHA512:RSA+SHA384:DSA+SHA384:ECDSA+SHA384:RSA+SHA256:DSA+S
Shared Signature Algorithms: RSA+SHA512:DSA+SHA512:ECDSA+SHA512:RSA+SHA384:DSA+SHA384:ECDSA+SHA384:RSA+SHA25
Supported Elliptic Curves: P-256:P-521:brainpoolP512r1:brainpoolP384r1:P-384:brainpoolP256r1:secp256k1:B-571
Shared Elliptic curves: P-256:P-521:brainpoolP512r1:brainpoolP384r1:P-384:brainpoolP256r1:secp256k1:B-571:K
---
New, TLSv1/SSLv2, Cipher is OQSKEY-DEFAULT-ECDHE-RSA-AES256-GCM-SHA384
SSL-Session:
  Protocol : TLSv1.2
  Cipher   : OQSKEY-DEFAULT-ECDHE-RSA-AES256-GCM-SHA384
  Session-ID:
  Session-ID-ctx: 01000000
  Master-Key: 27FC5115708287A283348723BB02A7FC135F499E23903AE243419C71CA616F74A7686B23DFE2AB780F093FEA99DF
  Key-Arg : None
  PSK identity: None
  PSK identity hint: None
  SRP username: None
  Start Time: 1542341524
  Timeout : 7200 (sec)
  Verify return code: 0 (ok)
---
0 items in the session cache
0 client connects (SSL_connect())
0 client renegotiates (SSL_connect())
0 client connects that finished
2 server accepts (SSL_accept())
0 server renegotiates (SSL_accept())
2 server accepts that finished
0 session cache hits
0 session cache misses
```

```
Ubuntu 18.04 Bionic (Fresh install, apt upgrade as of 2018/11/05) [Running]
Thu 23:12
dstebila@ds-ubuntu18: ~/Desktop/install
File Edit View Search Terminal Help
dstebila@ds-ubuntu18:~/Desktop/install$ bin/openssl s_server cert rsa.crt -key rsa.key -w
ww -tls1_2
Using default temp DH parameters
ACCEPT
ACCEPT
ACCEPT
Help
```

BoringSSL

- OQS fork of BoringSSL (which is a fork of OpenSSL)
 - PQ and hybrid key exchange in TLS 1.3
- After a few modifications, can be used with Chromium!

OQS demo: Chromium with BoringSSL talking to Apache

Main origin (non-secure)

▲ <https://localhost:4433>

This page is not secure (broken HTTPS).

▲ Certificate - **Subject Alternative Name missing**

The certificate for this site does not contain a Subject Alternative Name extension containing a domain name or IP address.

[View certificate](#)

▲ Certificate - **missing**

This site is missing a valid, trusted certificate (net::ERR_CERT_AUTHORITY_INVALID).

[View certificate](#)

■ Connection - **secure connection settings**

The connection to this site is encrypted and authenticated using TLS 1.3, oqs_kemdefault, and AES_256_GCM.

■ Resources - **all served securely**

All resources on this page are served securely.

OpenSSH

- OQS fork of OpenSSH
 - PQ and hybrid key exchange
 - PQ and hybrid signature authentication

OQS demo: OpenSSH

```
Ubuntu 16.04 Xenial (Fresh install, apt upgrade as of 2018/11/05) [Running]
Terminal File Edit View Search Terminal Help
10:40 PM
dstebila@ds-ubuntu16:~/Desktop/install$ ./run_ssh_client.sh
/home/dstebila/Desktop/install/bin/ssh -o KexAlgorithms=ecdh-nistp384-newhope-512-sha384@op
enquantumsafe.org -p 2222 10.0.1.29
dstebila@10.0.1.29's password:
Last login: Thu Nov 15 22:37:21 2018 from 10.0.2.2
Environment:
USER=dstebila
LOGNAME=dstebila
HOME=/home/dstebila
PATH=/usr/bin:/bin:/usr/sbin:/sbin:/home/dstebila/Desktop/install/bin
MAIL=/var/mail/dstebila
SHELL=/bin/bash
SSH_CLIENT=10.0.2.2 63692 2222
SSH_CONNECTION=10.0.2.2 63692 10.0.2.15 2222
SSH_TTY=/dev/pts/1
TERM=xterm-256color
dstebila@ds-ubuntu18:~$
```

```
Ubuntu 18.04 Bionic (Fresh install, apt upgrade as of 2018/11/05) [Running]
Thu 22:40
dstebila@ds-ubuntu18: ~/Desktop/install
File Edit View Search Terminal Help
debug1: sshd version OpenSSH_7.7, OpenSSL 1.0.2n 7 Dec 2017
debug1: private host key #0: ssh-rsa SHA256:gZBNb1fBmLJrt1ixRX7R0psN9gtuebcq0Px/xPPrOK8
debug1: private host key #1: ecdsa-sha2-nistp256 SHA256:4TK0050shRqFfFGMT7cktV3HTvBnPLZnf/
3SzQ6pBLU
debug1: private host key #2: ssh-ed25519 SHA256:9jh7ksWkYzh8haL9eAGWHCBiqWESCBGxsJv9AY99af
4
debug1: rexec_argv[0]='/home/dstebila/Desktop/install/sbin/sshd'
debug1: rexec_argv[1]='-p'
debug1: rexec_argv[2]='2222'
debug1: rexec_argv[3]='-d'
debug1: Set /proc/self/oom_score_adj from 0 to -1000
debug1: Bind to port 2222 on 0.0.0.0.
Server listening on 0.0.0.0 port 2222.
debug1: Bind to port 2222 on ::.
Server listening on :: port 2222.
debug1: Server will not fork when running in debugging mode.
debug1: rexec start in 5 out 5 newsock 5 pipe -1 sock 8
debug1: inetd sockets after dupping: 3, 3
Connection from 10.0.2.2 port 63692 on 10.0.2.15 port 2222
debug1: Client protocol version 2.0; client software version OpenSSH_7.7
debug1: match: OpenSSH_7.7 pat OpenSSH* compat 0x04000000
debug1: Local version string SSH-2.0-OpenSSH_7.7
debug1: permanently_set_uid: 1001/1001 [preauth]
debug1: list_hostkey_types: ssh-rsa,rsa-sha2-512,rsa-sha2-256,ecdsa-sha2-nistp256,ssh-ed25
519 [preauth]
debug1: SSH2_MSG_KEXINIT sent [preauth]
debug1: ShowApplications_KEXINIT received [preauth]
debug1: kex: algorithm: ecdh-nistp384-newhope-512-sha384@openquantumsafe.org [preauth]
```

Using OQS

— — —

- All open source software available on GitHub
- Instructions for building on Linux, macOS, and Windows
- Docker images available for building and running OQS-reliant applications
 - Apache httpd
 - curl
 - nginx
 - OpenSSH

Prototyping post-quantum and hybrid key exchange and authentication in TLS and SSH

Eric Crockett, Christian Paquin, Douglas Stebila. **Prototyping post-quantum and hybrid key exchange and authentication in TLS and SSH**. In *NIST 2nd Post-Quantum Cryptography Standardization Conference 2019*. August 2019. <https://eprint.iacr.org/2019/858>

Case study 1: TLS 1.2 in Amazon s2n

- Multi-level negotiation following TLS 1.2 design style:
 - Top-level ciphersuite with algorithm family: e.g.
TLS_**ECDHE_SIKE**_ECDSA_WITH_AES_256_GCM_SHA384
 - Extensions used to negotiate parameterization within family:
 - 1 extension for which ECDH elliptic curve: nistp256, curve25519, ...
 - 1 extension for which PQ parameterization: sikep403, sikep504, ...
- Session key: concatenate session keys and apply KDF with public key/ciphertext as KDF label
- Experimental results: successfully implemented using nistp256+{bike1l1, sikep503}

Case studies 2, 3, 4:

TLS 1.2 in OpenSSL 1.0.2

TLS 1.3 in OpenSSL 1.1.1

SSH v2 in OpenSSH 7.9

— — —

- Negotiate pairs of algorithms in pre-defined combinations
- Session key: concatenate session keys and use directly in key schedule
- Easy implementation, no change to negotiation logic
- Based on implementations in liboqs
 - KEMs: 9 of 17 (BIKE round 1, FrodoKEM, Kyber, LEDAcrypt, NewHope, NTRU, NTS (1 variant), Saber, SIKE)
 - Signature schemes: 6 of 9 (Dilithium, MQDSS, Picnic, qTesla (round 1), Rainbow, SPHINCS+)

1st circle: PQ only
 2nd circle: hybrid ECDH

● = success

◐ = fixable by changing implementation parameter

○ = would violate spec or otherwise unresolved error

† = algorithm on testing branch

	s2n (TLS 1.2)	OpenSSL 1.0.2 (TLS 1.2)	OpenSSL 1.1.1 (TLS 1.3)	OpenSSH
BIKE1-L1 (round 1)	●	●●	●●	●●
BIKE1-L3 (round 1)	--	●●	●●	●●
BIKE1-L5 (round 1)	--	●●	●●	●●
BIKE2-L1 (round 1)	--	●●	●●	●●
BIKE2-L3 (round 1)	--	●●	●●	●●
BIKE2-L5 (round 1)	--	●●	●●	●●
BIKE3-L1 (round 1)	--	●●	●●	●●
BIKE3-L3 (round 1)	--	●●	●●	●●
BIKE3-L5 (round 1)	--	●●	●●	●●
FrodoKEM-640-AES	--	●●	●●	●●
FrodoKEM-640-SHAKE	--	●●	●●	●●
FrodoKEM-976-AES	--	●●	●●	●●
FrodoKEM-976-SHAKE	--	●●	●●	●●
FrodoKEM-1344-AES	--	◐◐	◐◐	●●
FrodoKEM-1344-SHAKE	--	◐◐	◐◐	●●
Kyber512	--	●●	●●	●●
Kyber768	--	●●	●●	●●
Kyber1024	--	●●	●●	●●
LEDAcrypt-KEM-LT-12 [†]	--	●●	●●	●●
LEDAcrypt-KEM-LT-32 [†]	--	●●	●●	●●
LEDAcrypt-KEM-LT-52 [†]	--	●●	●●	●●
NewHope-512-CCA	--	●●	●●	●●
NewHope-1024-CCA	--	●●	●●	●●
NTRU-HPS-2048-509	--	●●	●●	●●
NTRU-HPS-2048-677	--	●●	●●	●●
NTRU-HPS-4096-821	--	●●	●●	●●
NTRU-HRSS-701	--	●●	●●	●●
NTS-KEM(12,64) [†]	--	○○	○○	○○
LightSaber-KEM	--	●●	●●	●●
Saber-KEM	--	●●	●●	●●
FireSaber-KEM	--	●●	●●	●●
SIKEp503 (round 1)	●	--	--	--
SIKEp434	--	●●	●●	●●
SIKEp503	--	●●	●●	●●
SIKEp610	--	●●	●●	●●
SIKEp751	--	●●	●●	●●

FrodoKEM 976, 1344

- OpenSSL 1.0.2 / TLS 1.2: too large for a pre-programmed buffer size, but easily fixed by increasing one buffer size
- OpenSSL 1.1.1 / TLS 1.3: same

NTS-KEM

- OpenSSL 1.0.2 / TLS 1.2: theoretically within spec's limitation of 2²⁴ bytes, but buffer sizes that large caused failures we couldn't track down
- OpenSSL 1.1.1 / TLS 1.3: too large for spec (2¹⁶-1 bytes)
- OpenSSH: theoretically within spec but not within RFC's "SHOULD", but couldn't resolve bugs

OpenSSL 1.1.1 (TLS 1.3)

Dilithium-2	●●
Dilithium-3	●●
Dilithium-4	●●
MQDSS-31-48	○●
MQDSS-31-64	○●
Picnic-L1-FS	○●
Picnic-L1-UR	○●
Picnic-L3-FS	○○
Picnic-L3-UR	○○
Picnic-L5-FS	○○
Picnic-L5-UR	○○
Picnic2-L1-FS	●●
Picnic2-L3-FS	○●
Picnic2-L5-FS	○●
qTesla-I (round 1)	●●
qTesla-III-size (round 1)	●●
qTesla-III-speed (round 1)	●●
Rainbow-Ia-Classic [†]	○●
Rainbow-Ia-Cyclic [†]	●●
Rainbow-Ia-Cyclic-Compressed [†]	●●
Rainbow-IIIc-Classic [†]	○●
Rainbow-IIIc-Cyclic [†]	○●
Rainbow-IIIc-Cyclic-Compressed [†]	○●
Rainbow-Vc-Classic [†]	○●
Rainbow-Vc-Cyclic [†]	○●
Rainbow-Vc-Cyclic-Compressed [†]	○●
SPHINCS+-{Haraka,SHA256,SHAKE256}-128f-{robust,simple}	○●
SPHINCS+-{Haraka,SHA256,SHAKE256}-128s-{robust,simple}	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-192f-{robust,simple}	○●
SPHINCS+-{Haraka,SHA256,SHAKE256}-192s-{robust,simple}	○●
SPHINCS+-{Haraka,SHA256,SHAKE256}-256f-{robust,simple}	○●
SPHINCS+-{Haraka,SHA256,SHAKE256}-256s-{robust,simple}	○●

TLS 1.3:

- Max certificate size: $2^{24}-1$
- Max signature size: $2^{16}-1$

OpenSSL 1.1.1:

- Max certificate size: 102,400 bytes, but runtime enlargeable
- Max signature size: 2^{14}

1st circle: PQ only

2nd circle: hybrid RSA

● = success

○ = fixable by changing implementation parameter

○ = would violate spec or otherwise unresolved error

† = algorithm on testing branch

	OpenSSL 1.1.1 (TLS 1.3)	OpenSSH
Dilithium-2	●●	●●
Dilithium-3	●●	●●
Dilithium-4	●●	●●
MQDSS-31-48	⊖⊖	●●
MQDSS-31-64	⊖⊖	●●
Picnic-L1-FS	⊖⊖	●●
Picnic-L1-UR	⊖⊖	●●
Picnic-L3-FS	○○	●●
Picnic-L3-UR	○○	●●
Picnic-L5-FS	○○	●●
Picnic-L5-UR	○○	●●
Picnic2-L1-FS	●●	●●
Picnic2-L3-FS	⊖⊖	●●
Picnic2-L5-FS	⊖⊖	●●
qTesla-I (round 1)	●●	●●
qTesla-III-size (round 1)	●●	●●
qTesla-III-speed (round 1)	●●	●●
Rainbow-Ia-Classic [†]	⊖⊖	⊖⊖
Rainbow-Ia-Cyclic [†]	●●	●●
Rainbow-Ia-Cyclic-Compressed [†]	●●	●●
Rainbow-IIIc-Classic [†]	⊖⊖	○○
Rainbow-IIIc-Cyclic [†]	⊖⊖	○○
Rainbow-IIIc-Cyclic-Compressed [†]	⊖⊖	○○
Rainbow-Vc-Classic [†]	⊖⊖	○○
Rainbow-Vc-Cyclic [†]	⊖⊖	○○
Rainbow-Vc-Cyclic-Compressed [†]	⊖⊖	○○
SPHINCS+-{Haraka,SHA256,SHAKE256}-128f-{robust,simple}	⊖⊖	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-128s-{robust,simple}	●●	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-192f-{robust,simple}	⊖⊖	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-192s-{robust,simple}	⊖⊖	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-256f-{robust,simple}	⊖⊖	●●
SPHINCS+-{Haraka,SHA256,SHAKE256}-256s-{robust,simple}	⊖⊖	●●

1st circle: PQ only

2nd circle: hybrid RSA

● = success

⊖ = fixable by changing implementation parameter

○ = would violate spec or otherwise unresolved error

† = algorithm on testing branch



OpenSSH maximum packet size: 2¹⁸

Summary

— — —

- Several design choices for hybrid key exchange in network protocols on negotiation and transmitting public keys, no consensus
- Protocols have size constraints which prevent some schemes from being used
- Implementations may have additional size constraints which affect some schemes, which can be bypassed with varying degrees of success

Extensions and open questions

— — —

Remaining Round 2 candidates

- Welcome help in getting code into our framework – either directly into liboqs or via PQClean

Constraints in other parts of the protocol ecosystem

- Other client/server implementations
- Middle boxes

Performance

- Latency and throughput in lab conditions
- Latency in realistic network conditions à la [Lan18]

Use in applications

- Tested our OpenSSL experiment with Apache, nginx, links, OpenVPN, with reasonable success
- More work to do:
S/MIME, more TLS clients, ...

Benchmarking PQ crypto in TLS

Christian Paquin, Douglas Stebila, Goutam Tamvada. **Benchmarking post-quantum cryptography in TLS**. November, 2019. <https://eprint.iacr.org/2019/1447>

Prior Work

2016

Google, with
NewHope in
TLS 1.2



2018

Google, with
“dummy
extensions”



2019

Google and
Cloudflare, with
SIKE and NTRU-
HRSS in TLS 1.3

**What if you
don't have
billions of clients
and
millions of servers?**

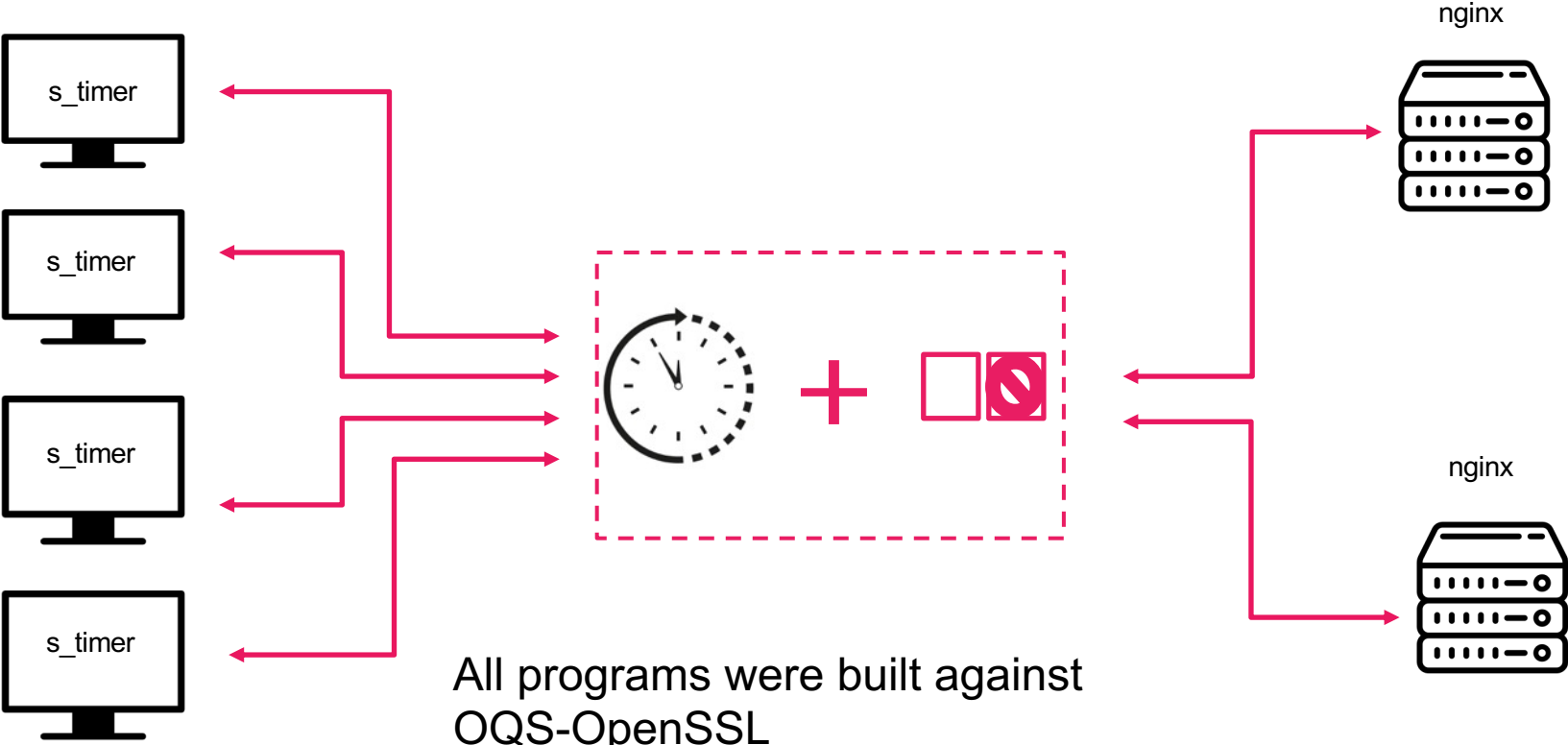
Emulate the network

+ more control over
experiment parameters

+ easier to isolate
effects of network
characteristics

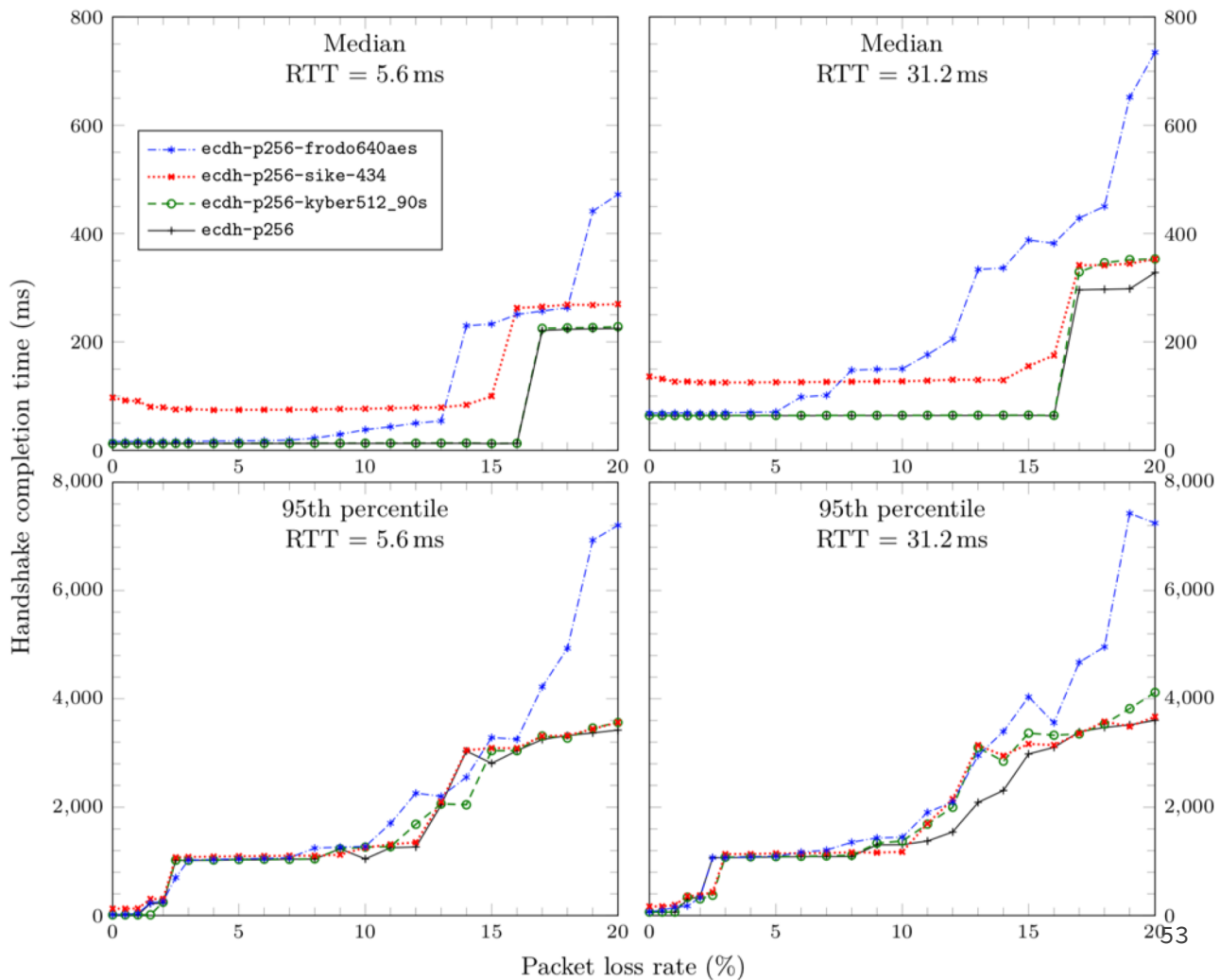
– loss in realism

Experiment setup



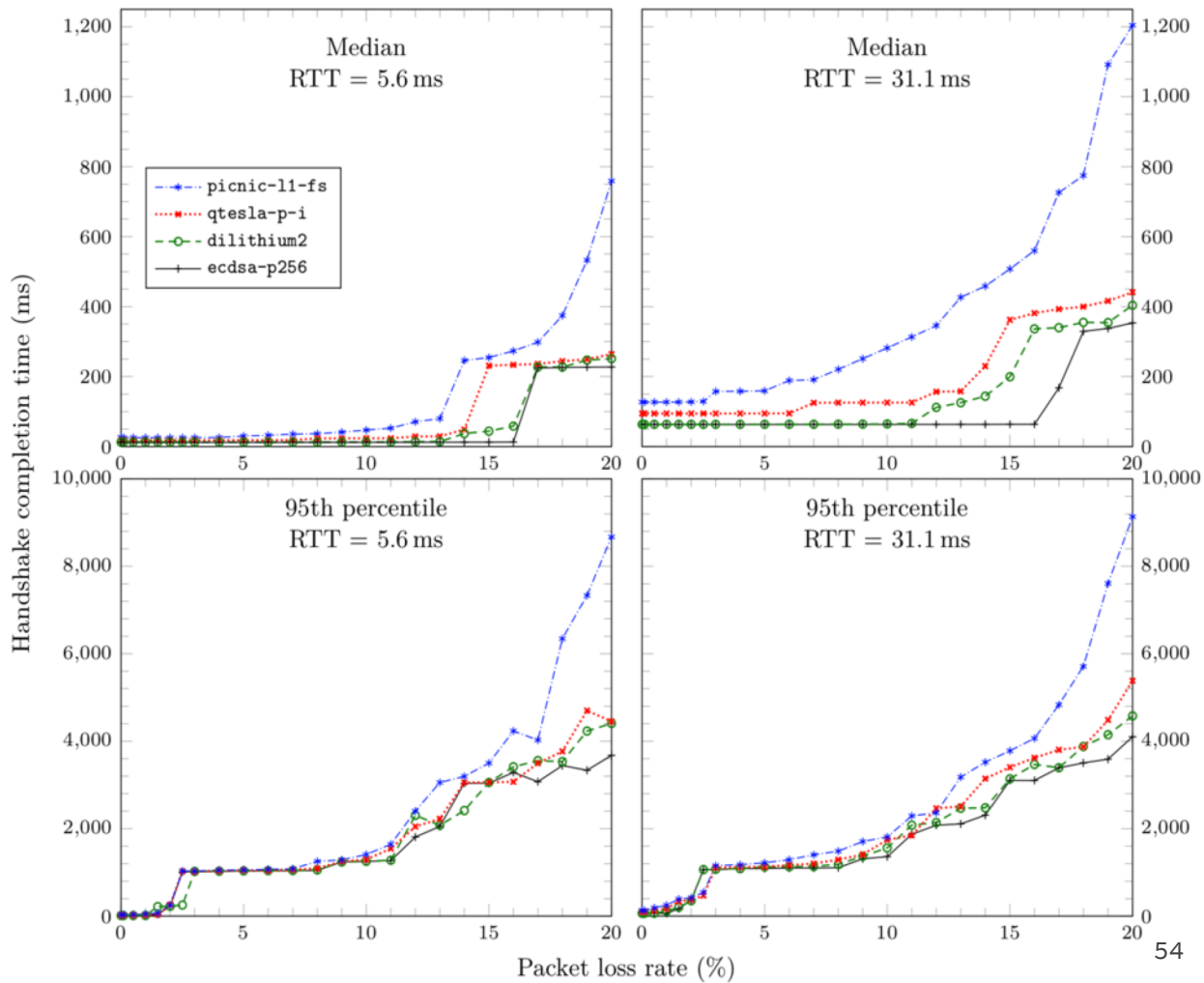
Key exchange

handshake latency
as a function of
packet loss rate



Authentication

handshake latency
as a function of
packet loss rate



Challenges in proving post-quantum key exchanges based on key encapsulation mechanisms

Jacqueline Brendel, Marc Fischlin, Felix Günther, Christian Janson, Douglas Stebila. **Challenges in proving post-quantum key exchanges based on key encapsulation mechanisms**. Technical report. November 2019. <https://eprint.iacr.org/2019/1356>

Implicitly authenticated key exchange

— — —

Idea: Use **static DH + ephemeral DH** rather than signatures + ephemeral DH

Examples:

- TLS 1.2 static DH
- OPTLS (predecessor to TLS 1.3)
- Signal X3DH handshake
- QUIC original handshake
- Many protocols in the academic literature

PQ: Use **long-term KEM + ephemeral KEM** rather than signatures + ephemeral KEM

- Potentially save space since many PQ signatures are bigger than PQ KEMs

DH is too awesome

— — —

Diffie–Hellman is very flexible:

- Different message flows:
serial versus parallel
- Key reuse
- Same cryptographic object for
different purposes
- Range of cryptographic
assumptions:
from plain CDH and DDH
up to interactive PRF-ODH

KEMs are not flexible:

- Encapsulator needs to know the
public key against which they're
encapsulating
- Most PQ KEMs not secure against
key reuse without protection
(Fujisaki–Okamoto transform)
- No known efficient methods for
static–static KEM agreement (FO
transform gets in the way)

Case study: TLS 1.3

Client

Server

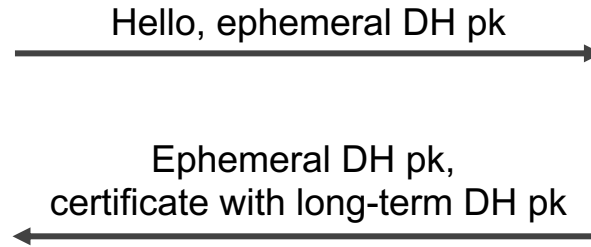
Hello, ephemeral DH pk

Ephemeral DH pk,
certificate with long-term signing pk,
signature

Case study: TLS 1.3 **implicitly authenticated DH**

Client

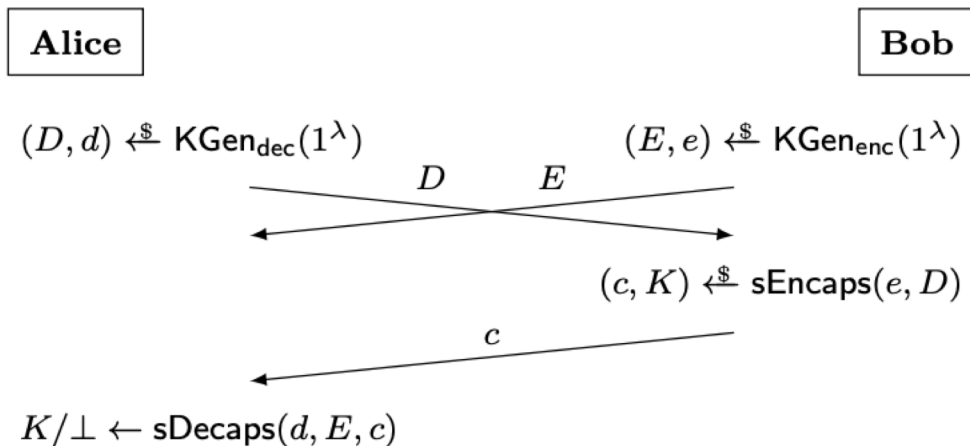
Server



Session key = $H(\text{ephemeral-ephemeral}, \text{ephemeral-static})$

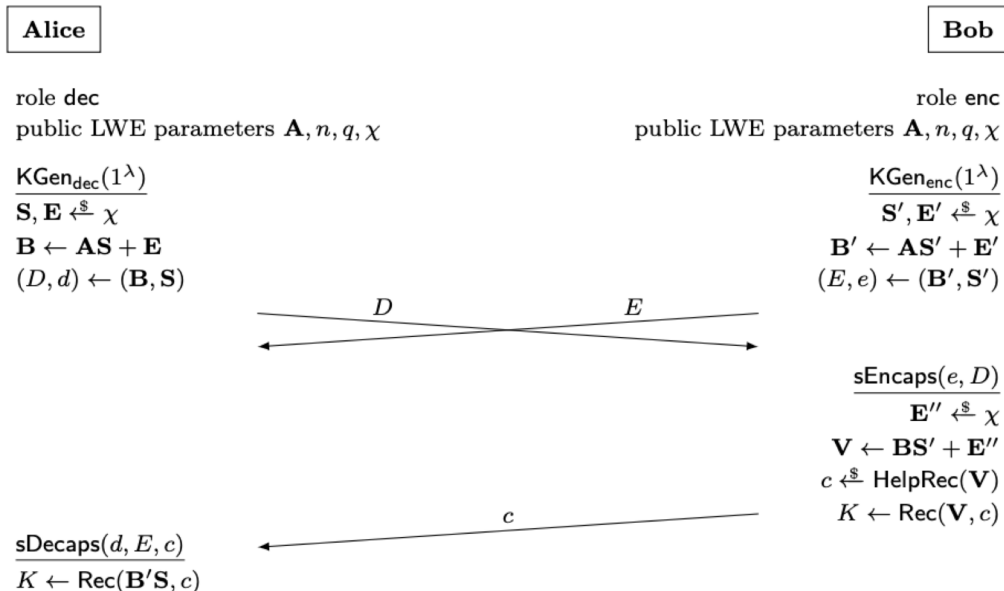
Idea: “split KEMs”

- Some LWE-based KEMs (Lindner–Peikert/Ding style) have ciphertexts part of which could be treated as a public key
- So order of public key and encapsulation could be partially swapped or separated



LWE as a split KEM

- Some LWE-based KEMs (Lindner–Peikert/Ding style) have ciphertexts part of which could be treated as a public key
- So order of public key and encapsulation could be partially swapped or separated
- **Not a full solution: couldn't figure out how to achieve active (CCA) security without FO transform**



Wrapping up

Some questions for adoption

- Hybrid key exchange:
2 or ≥ 2 algorithms?
- What level of
network
performance is
acceptable?



Some questions for academia

- Is it safe to use an IND-CPA KEM for ephemeral key exchange in TLS 1.3?
- Can CCA-secure split KEMs be
instantiated?

Exploring post-quantum cryptography in Internet protocols

Douglas Stebila



UNIVERSITY OF
WATERLOO



**NSERC
CRSNG**

<https://eprint.iacr.org/2019/858>

<https://eprint.iacr.org/2019/1356>

<https://eprint.iacr.org/2019/1447>

<https://tools.ietf.org/html/draft-stebila-tls-hybrid-design-01>

<https://openquantumsafe.org/>

<https://github.com/open-quantum-safe/>

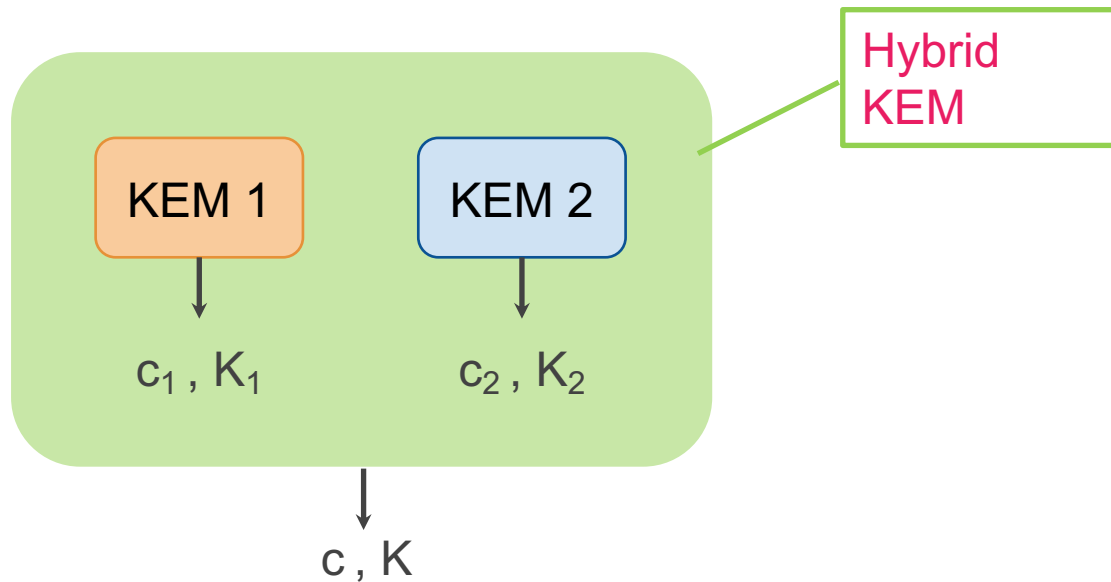
<https://www.douglas.stebila.ca/>

Appendix

Hybrid key encapsulation mechanisms and authenticated key exchange

Nina Bindel, Jacqueline Brendel, Marc Fischlin, Brian Goncalves, Douglas Stebila. **Hybrid key encapsulation mechanisms and authenticated key exchange**. In Jintai Ding, Rainer Steinwandt, editors, *Proc. 10th International Conference on Post-Quantum Cryptography (PQCrypto) 2019, LNCS*. Springer, May 2019. <https://eprint.iacr.org/2019/858>

Safely combining KEMs



- How to safely combine into single KEM such that this hybrid preserves security, as long as one of the two input schemes remains secure

Existing options

— — —

- XOR
 - $K = K1 \text{ XOR } K2$
 - Preserves IND-CPA security but not IND-CCA security (mix and match attack)
- XOR with transcript (Giacon et al. PKC 2018)
 - $K = H(K1 \text{ XOR } K2, C1 \parallel C2)$
 - Preserves IND-CCA security if H is a random oracle
- Concatenation (Giacon et al. PKC 2018)
 - $K = H(K1 \parallel K2, C1 \parallel C2)$
 - Preserves IND-CCA security if H is a random oracle

The XOR-then-MAC Combiner

- Add MAC $\tau = \text{MAC}(c)$

$$K \parallel K_{\text{MAC}} \leftarrow K_1 \text{ XOR } K_2$$

$$c = (c_1, c_2, \tau)$$

- Preserves IND-CCA security under the **standard model** assumption that MAC is secure
- Protocols (e.g. TLS) often compute MAC over transcript anyways (may replace the MAC here)

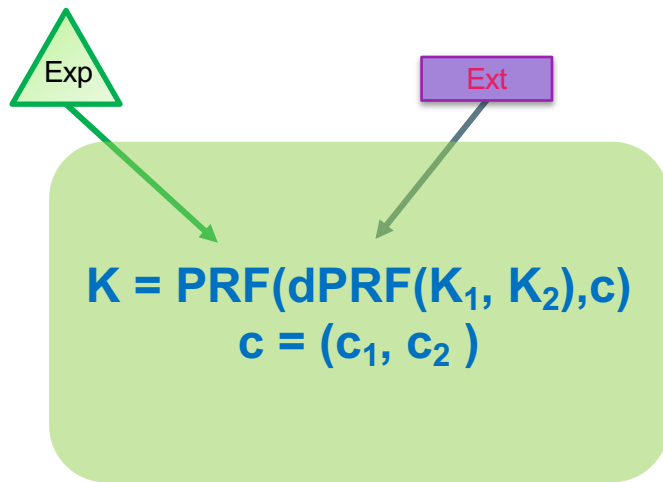
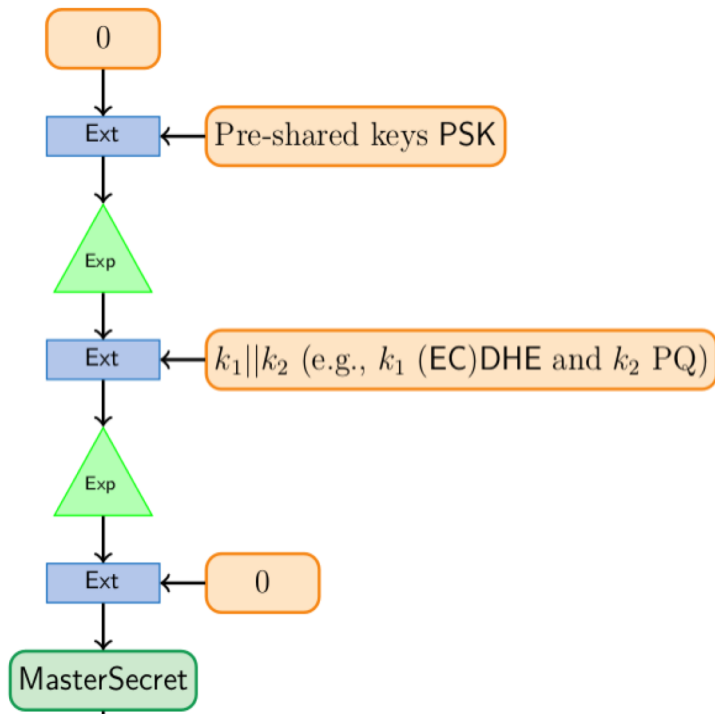
dualPRF Combiner

— — —

- **dualPRF Security:** both $\text{dPRF}(k, \cdot)$ and $\text{dPRF}(\cdot, x)$ are pseudorandom functions
- Models concatenation-based TLS 1.3 hybrid drafts
- HKDF is a dual PRF

$$\begin{aligned} K &= \text{PRF}(\text{dPRF}(K_1, K_2), c) \\ c &= (c_1, c_2) \end{aligned}$$

dualPRF Combiner

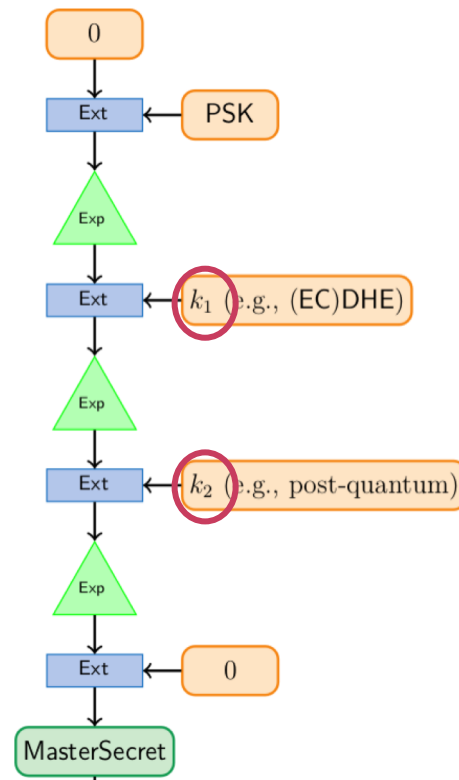


Nested dualPRF Combiner

- dualPRF combiner with additional preprocessing step
- Inspired by the TLS 1.3 key schedule
 - Models TLS 1.3 hybrid draft by Schanck and Stebila

$$K_e = \text{Ext}(0, K_1)$$

$$K = \text{PRF}(\text{dPRF}(K_e, K_2), c)$$



Design issues for hybrid key exchange in TLS 1.3

Douglas Stebila, Scott Fluhrer, Shay Gueron. **Design issues for hybrid key exchange in TLS 1.3. Internet-Draft.** Internet Engineering Task Force, July 2019. <https://tools.ietf.org/html/draft-stebila-tls-hybrid-design-01>

Candidate Instantiation 1 – Negotiation

Follows draft-whyte-qsh-tls13-06

NamedGroup enum for supported_groups extension contains “hybrid markers” with no pre-defined meaning

Each hybrid marker points to a mapping in an extension, which lists which combinations the client proposes; between 2 and 10 algorithms permitted

supported_groups:

hybrid_marker00, hybrid_marker01, hybrid_marker02, secp256r1

HybridExtension:

- hybrid_marker00 → secp256r1+sike123+ntru456
- hybrid_marker01 → secp256r1+sike123
- hybrid_marker02 → secp256r1+ntru456

Candidate Instantiation 1 – Conveying keyshares

Client's key shares:

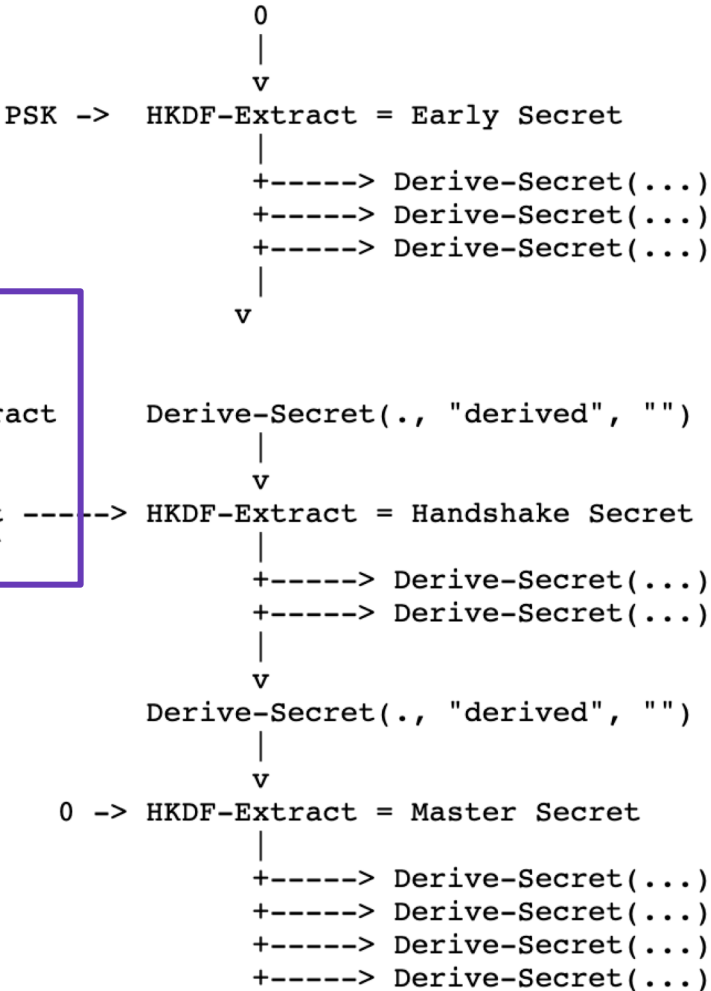
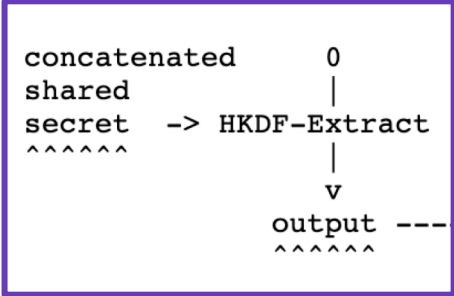
- Existing KeyShareClientHello allows multiple key shares
- => Send 1 key share per algorithm
 - secp256r1, sike123, ntru456
- No changes required to data structures or logic

Server's key shares:

- Respond with NamedGroup = hybrid_markerXX
- Existing KeyShareServerHello only permits one key share
- => Squeeze 2+ key shares into single key share field by concatenation

```
struct {  
    KeyShareEntry key_share<2..10>;  
} HybridKeyShare;
```

Instantiation 1 – Combining keys



Candidate Instantiation 2 – Negotiation

Follows draft-kiefer-tls-ecdhe-sidh-00, enum {
Open Quantum Safe implementation, ...

New NamedGroup element
standardized for each desired
combination

No internal structure to new code
points

```
enum {  
    /* existing named groups */  
    secp256r1 (23),  
    x25519 (0x001D),  
    ...,  
  
    /* new code points eventually defined for post-quantum algorithms */  
    PQ1 (0x????),  
    PQ2 (0x????),  
    ...,  
  
    /* new code points defined for hybrid combinations */  
    secp256r1_PQ1 (0x????),  
    secp256r1_PQ2 (0x????),  
    x25519_PQ1 (0x????),  
    x25519_PQ2 (0x????),  
  
    /* existing reserved code points */  
    ffdhe_private_use (0x01FC..0x01FF),  
    ecdhe_private_use (0xFE00..0xFEFF),  
    (0xFFFF)  
} NamedGroup;
```

Candidate Instantiation 2 – Conveying keyshares

KeyShareClientHello contains an entry for each code point listed in supported_groups

KeyShareServerHello contains a single entry for the chosen code point

KeyShareEntry for hybrid code points is an opaque string parsed with the following internal structure:

```
struct {  
    KeyShareEntry key_share<2..10>;  
} HybridKeyShare;
```


Candidate Instantiation 1

Adds new negotiation logic and ClientHello extensions

Does not result in duplicate key shares or combinatorial explosion of NamedGroups

Candidate Instantiation 2

No change in negotiation logic or data structures

No change to protocol logic: concatenation of key shares and KDFing shared secrets can be handled “internally” to a method

Results in combinatorial explosion of NamedGroups

Duplicate key shares will be sent

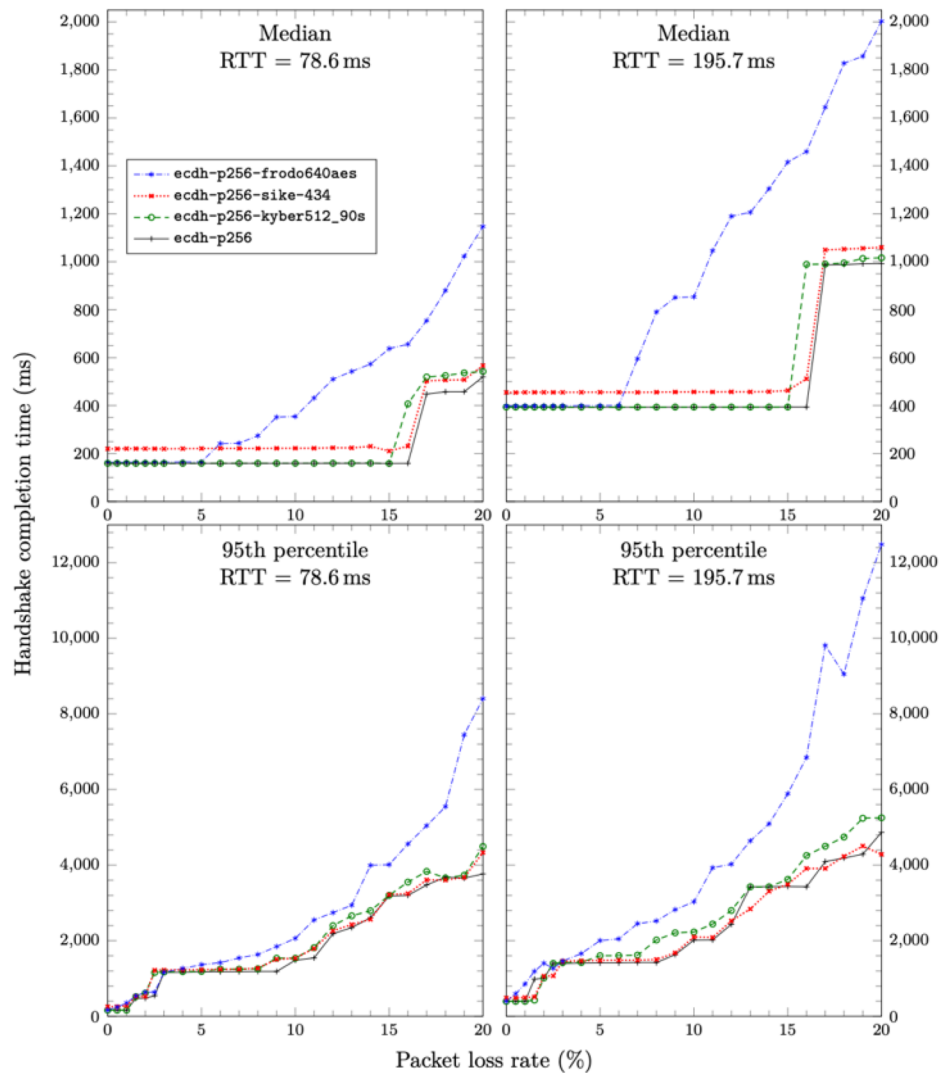
Benchmarking PQ crypto in TLS

Christian Paquin, Douglas Stebila, Goutam Tamvada. **Benchmarking post-quantum cryptography in TLS**. November, 2019. <https://eprint.iacr.org/2019/1447>

Key exchange

handshake latency
as a function of packet
loss rate

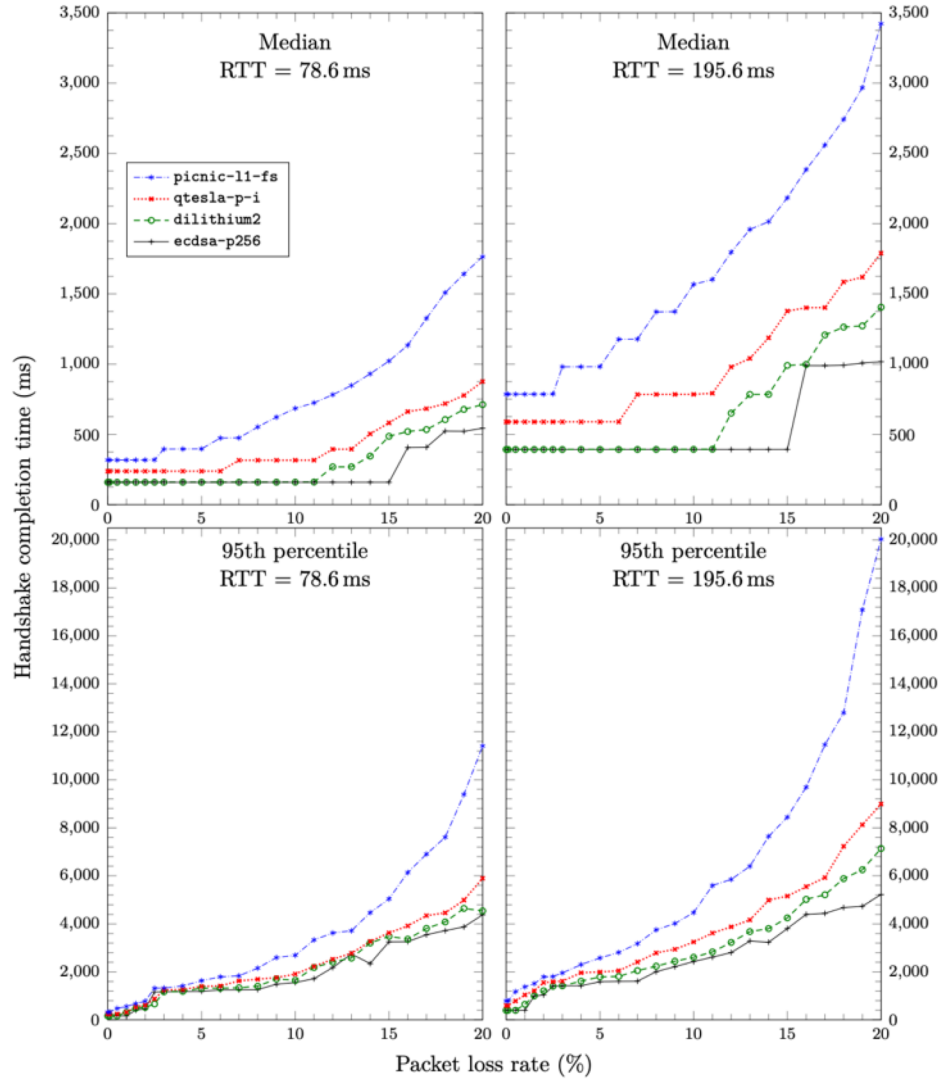
higher network latency



Authentication

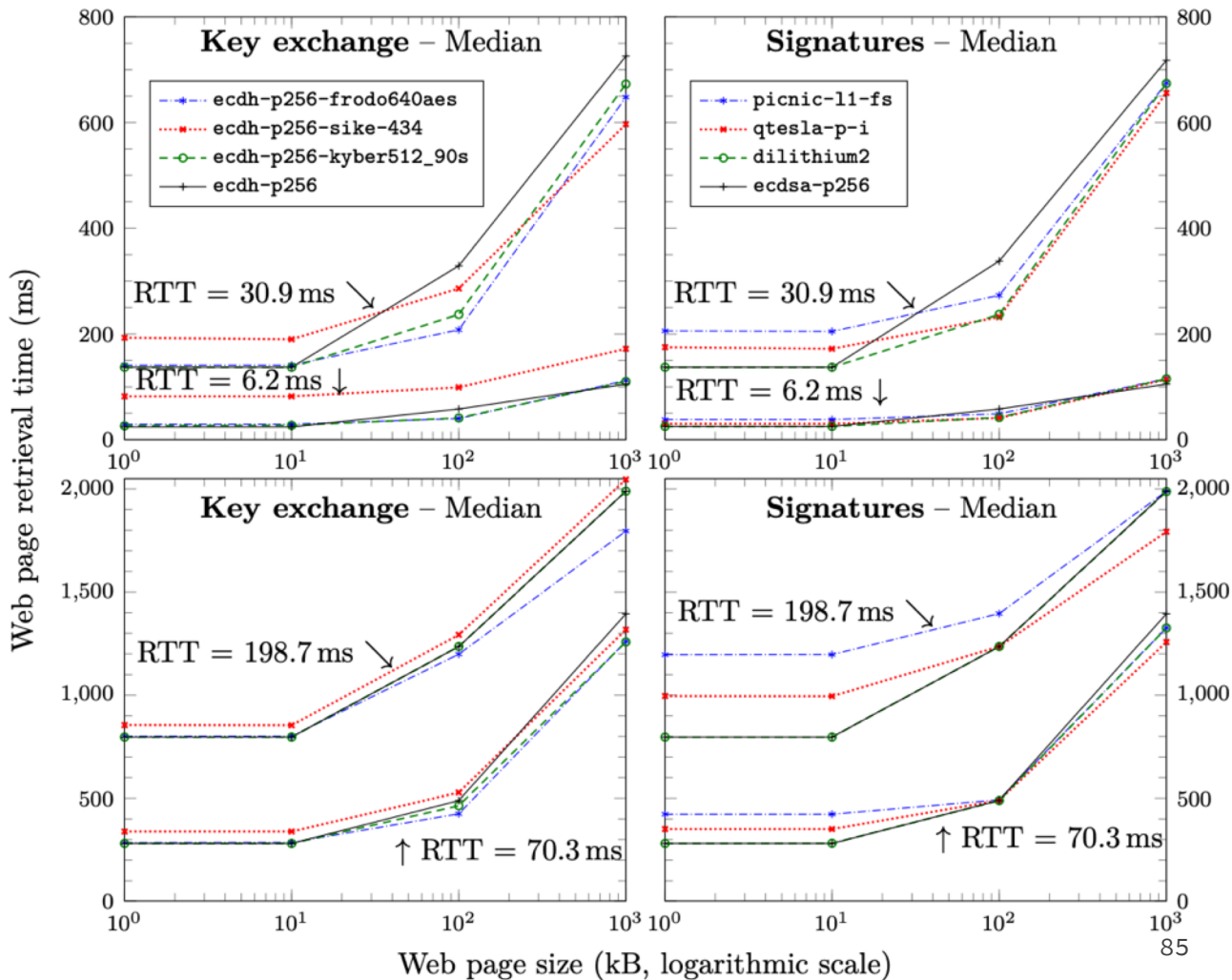
handshake latency
as a function of packet
loss rate

higher network latency



Data-centre- to-data-centre

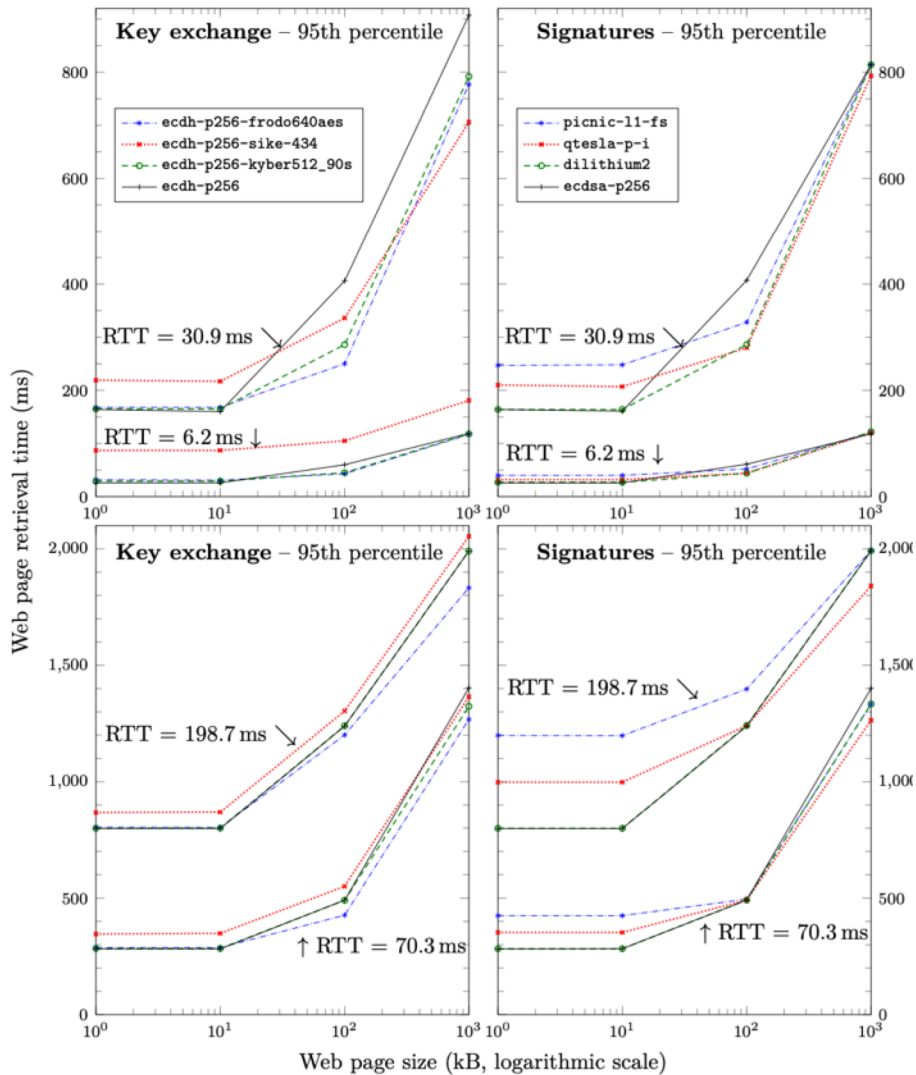
web page latency
as a function of
page size



Data-centre- to-data-centre

web page latency
as a function of
page size

higher network
latency



Challenges in proving post-quantum key exchanges based on key encapsulation mechanisms

Jacqueline Brendel, Marc Fischlin, Felix Günther, Christian Janson, Douglas Stebila. **Challenges in proving post-quantum key exchanges based on key encapsulation mechanisms**. Technical report. November 2019. <https://eprint.iacr.org/2019/1356>

Protocol	Core message flow	Session key	Security
SSHv2 signed ephemeral DH	$ \begin{array}{c} \xrightarrow{\text{hello}} \\ \xleftarrow{\text{hello}} \\ \xrightarrow{\text{epk}_A} \\ \xrightarrow{\text{epk}_B, \text{lpk}_B, \text{sig}} \\ \xleftarrow{\hspace{1.5cm}} \end{array} $	$\text{DH}(\text{epk}_A, \text{epk}_B)$	DDH [4]
TLS 1.2 signed ephemeral DH	$ \begin{array}{c} \xrightarrow{\text{hello}} \\ \xleftarrow{\text{epk}_B, \text{cert}(\text{lpk}_B), \text{sig}} \\ \xrightarrow{\text{epk}_A} \\ \xrightarrow{\hspace{1.5cm}} \end{array} $	$\text{DH}(\text{epk}_A, \text{epk}_B)$	snPRF-ODH [32]
TLS 1.3 signed ephemeral DH	$ \begin{array}{c} \xrightarrow{\text{hello}, \text{epk}_A} \\ \xleftarrow{\text{epk}_B, \text{cert}(\text{lpk}_B), \text{sig}} \\ \xleftarrow{\hspace{1.5cm}} \end{array} $	$\text{DH}(\text{epk}_A, \text{epk}_B)$	snPRF-ODH [22]

Protocol	Core message flow	Session key	Security
TLS 1.2 [12] (implicitly-auth static Diffie–Hellman + explicit-auth MAC)	$\begin{array}{c} \xrightarrow{\text{hello}} \\ \xleftarrow{\text{cert}[lpk_B], \text{mac}} \\ \xrightarrow{epk_A, \text{mac}} \end{array}$	$\text{DH}(epk_A, lpk_B)$	mnPRF-ODH [36]
OPTLS [37] (TLS 1.3–style, implicitly-auth Diffie–Hellman + explicit-auth MAC)	$\begin{array}{c} \xrightarrow{\text{hello}, epk_A} \\ \xleftarrow{epk_B, \text{cert}[lpk_B], \text{mac}} \end{array}$	$\text{DH}(epk_A, epk_B)$ $\parallel \text{DH}(epk_A, lpk_B)$	GapDH, DDH [37] (random oracle model)
Signal [54] X3DH triple handshake [+ optional ephemeral-ephemeral]	$\begin{array}{c} \xrightarrow{\text{hello}} \\ \xleftarrow{lpk_B, sspk_B, [epk_B]} \\ \xrightarrow{lpk_A, epk_A} \end{array}$	$\text{DH}(lpk_A, sspk_B)$ $\parallel \text{DH}(epk_A, lpk_B)$ $\parallel \text{DH}(epk_A, sspk_B)$ $\parallel [\text{DH}(epk_A, epk_B)]$	mmPRF-ODH, smPRF-ODH, smPRF-ODH, [snPRF-ODH] [7]
QUIC original handshake [41]	$\begin{array}{c} \xrightarrow{\text{hello}, epk_A} \\ \xleftarrow{sspk_B} \end{array}$	$\text{DH}(epk_A, lpk_B)$ $\parallel \text{DH}(epk_A, sspk_B)$	GapDH [25] (random oracle model)

Signal X3DH handshake

Alice

Signal Server

Bob

identity A

static identity key (lpk_A, lsk_A)

semi-static prekey $(ssp_k_A, sssk_A)$

(opt.) eph. prekeys $\{(epk_A^i, epsk_A^i)\}_i$

identity B

static identity key (lpk_B, lsk_B)

semi-static prekey $(ssp_k_B, sssk_B)$

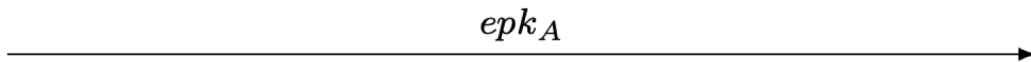
(opt.) eph. prekeys $\{(epk_B^i, epsk_B^i)\}_i$



$(epk_A, esk_A) \xleftarrow{\$} \text{KGen}(1^\lambda)$

$ms \leftarrow ssp_k_B^{lsk_A} || lpk_B^{esk_A} || ssp_k_B^{esk_A} || eppk_B^{esk_A}$

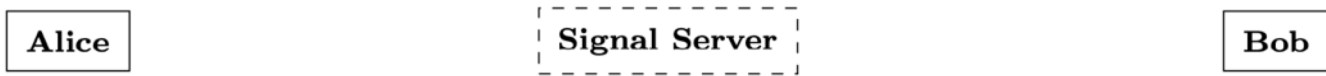
$K \leftarrow F(ms, \cdot)$



$ms \leftarrow lpk_A^{sssk_B} || epk_A^{lsk_B} || epk_A^{sssk_B} || epk_A^{epsk_B}$

$K \leftarrow F(ms, \cdot)$

Signal handshake with KEMs

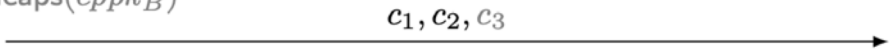


identity A
 static identity key (lpk_A, lsk_A)
 semi-static prekey $(sspk_A, sssk_A)$
 (opt.) eph. prekeys $\{(eppk_A^i, epsk_A^i)\}_i$

identity B
 static identity key (lpk_B, lsk_B)
 semi-static prekey $(sspk_B, sssk_B)$
 (opt.) eph. prekeys $\{(eppk_B^i, epsk_B^i)\}_i$



$(c_1, K_1) \xleftarrow{\$} \text{Encaps}(lpk_B)$
 $(c_2, K_2) \xleftarrow{\$} \text{Encaps}(sspk_B)$
 $(c_3, K_3) \xleftarrow{\$} \text{Encaps}(eppk_B)$



$K_1 \leftarrow \text{Decaps}(sssk_B, c_1)$
 $K_2 \leftarrow \text{Decaps}(lsk_B, c_2)$
 $K_3 \leftarrow \text{Decaps}(epsk_B, c_3)$
 $(c_4, K_4) \xleftarrow{\$} \text{Encaps}(lpk_A)$
 $ms \leftarrow K_4 || K_1 || K_2 || K_3$
 $K \leftarrow F(ms, \cdot)$



$K_4 \leftarrow \text{Decaps}(lsk_A, c_4)$
 $ms \leftarrow K_4 || K_1 || K_2 || K_3$
 $K \leftarrow F(ms, \cdot)$

Signal handshake with split KEMs

Alice

Signal Server

Bob

identity A
static identity key (lpk_A, lsk_A)
semi-static prekey $(sspk_A, sssk_A)$
(opt.) eph. prekeys $\{(eppk_A^i, epsk_A^i)\}_i$

identity B
static identity key (lpk_B, lsk_B)
semi-static prekey $(sspk_B, sssk_B)$
(opt.) eph. prekeys $\{(eppk_B^i, epsk_B^i)\}_i$

$lpk_B, sspk_B, epk_B$ lpk_A

$(epk_A, esk_A) \xleftarrow{\$} \text{KGen}(1^\lambda)$
 $(c_1, K_1) \xleftarrow{\$} \text{sEncaps}(lsk_A, sspk_B)$
 $(c_2, K_2) \xleftarrow{\$} \text{sEncaps}(esk_A, lpk_B)$
 $(c_3, K_3) \xleftarrow{\$} \text{sEncaps}(esk_A, sspk_B)$
 $(c_4, K_4) \xleftarrow{\$} \text{sEncaps}(esk_A, epk_B)$
 $ms \leftarrow K_1 || K_2 || K_3 || K_4$
 $K \leftarrow F(ms, \cdot)$

$epk_A, c_1, c_2, c_3, c_4$

$K_1 \leftarrow \text{sDecaps}(sssk_B, lpk_A, c_1)$
 $K_2 \leftarrow \text{sDecaps}(lsk_B, epk_A, c_2)$
 $K_3 \leftarrow \text{sDecaps}(sssk_B, epk_A, c_3)$
 $K_4 \leftarrow \text{sDecaps}(epsk_B, epk_A, c_4)$
 $ms \leftarrow K_1 || K_2 || K_3 || K_4$
 $K \leftarrow F(ms, \cdot)$